

**Kharazmi University**  
**Faculty of Physics**

شماره‌ی تکلیف: ۴

**Problem 1:**

Find the arc length of the function  $y = \frac{1}{2}(e^x + e^{-x})$  from  $x = -2$  to  $x = 2$ .

**Answer:**  $e^2 - e^{-2}$

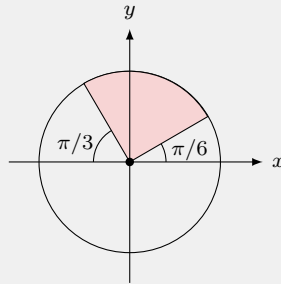
**Problem 2:**

Find the arc length of the function  $y = f(x) = \int_1^x \sqrt{x'^2 - 1} dx'$  from  $x = 2$  to  $x = 4$

**Answer:** 6

**Problem 3:**

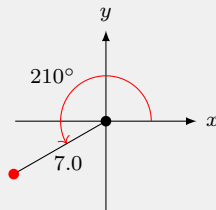
Consider a circular disk with radius  $a$ . Calculate the area of the portion of this circle that is enclosed between the angles  $\phi = \frac{\pi}{6}$  and  $\phi = \frac{2\pi}{3}$ .



**Answer:**  $\frac{\pi a^2}{4}$

**Problem 4:**

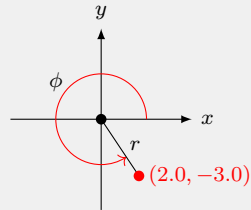
Find the cartesian coordinates of the point whose polar coordinates are  $(\rho, \phi) = (7.0, 210^\circ)$ .



**Answer:**  $\left(-\frac{7\sqrt{3}}{2}, -\frac{7}{2}\right) = (-6.06, -3.5)$

**Problem 5:**

Find the polar coordinates of the point whose cartesian coordinates are  $(x, y) = (2.0, -3.0)$ .



$(\rho, \phi) = ?$

**Answer:**  $\left(\sqrt{13}, 2\pi - \tan^{-1}\left(\frac{3}{2}\right)\right) = (3.61, 303.69^\circ)$